

# P P SAVANI UNIVERSITY

Third-Semester of B.Sc. (IT) Examination

December 2022

SESH2060 Statistics

23.11.2022, Wednesday

Time: 10:00 a.m. To 12:30 p.m.

Maximum Marks: 60

## Instructions:

1. The question paper comprises of two sections.
2. Section I and II must be attempted in separate answer sheets.
3. Make suitable assumptions and draw neat figures wherever required.
4. Use of scientific calculator is allowed.

## SECTION - I

- Q - 1** Answer the following. (Any Five) [05] CO BTL
- (i) Write the formula of simple variance. 1 1/2
- (ii) Write a difference between cross sectional data and time series data 1 1/2
- (iii) Write the definition of frequency distribution. 1 1/2
- (iv) Write definition of sample correlation. 1 1/2
- (v) The mean of 1, 2, 3, 4, 5 is \_\_\_\_\_. 1 1/2
- (vi) Write the formula of Counting rule for Permutation. 1 1/2
- (vii) Write the formula of Variance of a Discrete Random variable. 1 1/2
- Q - 2 (a)** Consider a sample with given data values 2, 3, 5, 21, 93, 99, 99, 102 [05] 1 5
- (i) Compute the mean, median and mode
- (ii) Compute the first quartile
- (iii) Compute the third quartile
- Q - 2 (b)** Discuss the scale of measurement with example. [05] 1 3/4
- OR
- Q - 2 (a)** Consider a sample with a mean of 500 and standard deviation of 100. [05] 1 5
- What is the Z score for the following data values:  
520, 650, 500, 450, 280
- Q - 2 (b)** Show the five number summary for the following data: [05] 1 5
- 27, 25, 20, 15, 30, 28, 25
- Q - 3 (a)** Consider a sample with a mean of 30 and a standard deviation of 5. Use [05] 1 3/5
- chebyshevs theorem to determine the percentage of the data within each of the following ranges:
- (i) 20 to 40 (ii) 18 to 42
- Q - 3 (b)** A bowler's score for six games were 182, 168, 184, 190, 170 and 174. Using [05] 5
- these data as a population, compute the following descriptive statistic:
- (i) Standard deviation
- (ii) Co-efficient of Variance
- OR
- Q - 3 (a)** Consider the following frequency distribution [05] 1 6
- | Class     | 10-19 | 20-29 | 30-39 | 40-49 | 50-59 |
|-----------|-------|-------|-------|-------|-------|
| Frequency | 10    | 14    | 17    | 7     | 2     |
- (i) Construct a cumulative frequency distribution and a cumulative relative frequency distribution.
- (ii) Construct a histogram and an Ogive.
- Q - 3 (b)** Consider a sample with the given data values and compute the Interquartile [05] 1 5
- range and standard deviation: 27, 25, 20, 15, 30, 34, 28 and 25.

- Q - 4 Attempt any one** [05] 1 3/5
- (a) Suppose the data have a bell-shaped distribution with a mean of 30 and a standard deviation of 5. Use the empirical rule to determine the percentage of data within each of the following ranges:
- (i) 15 to 45 (ii) 25 to 35
- (b) Calculate the sample correlation of the following data: 1 5

$x$	50	60	70	90	100
$y$	65	51	40	26	8

**SECTION - II**

- Q - 1 Answer the following (Any Five)** [05]
- (i) Write a formula of standard normal density function. 2 1/2
- (ii) Write a definition of Random variable. 2 1/2
- (iii) The sum of the probabilities must be \_\_\_\_\_. 2 1/2
- (iv) Write a definition of Discrete Random Variable. 2 1/2
- (v) Write two observations of Normal Probability Distribution. 2 1/2
- (vi) Write a formula of Poisson Probability Function. 2 1/2
- (vii) Write a formula of Sample Correlation. 2 1/2
- Q - 2 (a)** Bag I contain 4 white and 6 black balls while another Bag II contains 4 white and 3 black balls. One ball is drawn at random from one of the bags and it is found to be black. Find the probability that it was drawn from Bag I. [05] 2 5
- Q - 2 (b)** The following table provides a probability distribution for the random variable  $x$ . [05] 2 5

$x$	3	6	9
$f(x)$	0.25	0.50	0.25

- (i) Compute  $E(x)$ , the expected value of  $x$ .
- (ii) Compute  $\sigma^2$ , the variance of  $x$ .
- (iii) Compute  $\sigma$  the standard deviation of  $x$ .

**OR**

- Q - 2 (a)** Suppose that we have two events,  $A$  and  $B$ , with  $P(A) = 0.50$ ,  $P(B) = 0.60$ , and  $P(A \cap B) = 0.40$ . [05] 2 5
- (i) Find  $P(A|B)$
- (ii) Find  $P(B|A)$
- (iii) Are  $A$  and  $B$  independent? Why or why not?
- Q - 2 (b)** The probability distribution for the random variable  $x$  follows: [05] 2 5

$x$	20	25	30	35
$f(x)$	0.20	0.15	0.25	0.40

- (i) Is this probability distribution valid? Explain.
- (ii) What is the probability that  $x = 30$ ?
- (iii) What is the probability that  $x$  is less than or equal to 25?
- (iv) What is the probability that  $x$  is greater than 30?

**Q - 3 (a)** The distribution of wages of a group of workers is known to be normal with mean \$500 and standard deviation \$100. If the wages of 100 workers in the group are less than \$430. What is the total numbers of workers in the group? (Hint:  $P(0 < Z < 0.7) = 0.258$ ) [05] 2 5

**Q - 3 (b)** Consider a Poisson distribution with  $\mu = 3$ . [05] 2 5

- (i) Write the appropriate Poisson probability function.
- (ii) Compute  $f(2)$ .
- (iii) Compute  $f(1)$ .
- (iv) Compute  $P(x \geq 2)$ .

**OR**

**Q - 3 (a)** The random variable  $x$  is known to be uniformly distributed between 1.0 and 1.5 [05] 2 5

- (i) Show the graph of the probability density function.
- (ii) Compute  $P(x = 1.25)$ .
- (iii) Compute  $P(1.0 \leq x \leq 1.25)$ .
- (iv) Compute  $E(x)$ .

**Q - 3 (b)** An average of 15 aircraft accidents occur each year (The World Almanac and Book of Facts, 2004). [05] 2 5

Compute the mean number of aircraft accidents per month.

- (i) Compute the mean number of aircraft accidents per month.
- (ii) Compute the probability of no accidents during a month.
- (iii) Compute the probability of exactly one accident during a month.
- (iv) Compute the probability of more than one accident during a month.

**Q - 4 Attempt any one.** [05]

**(i)** In 1950 in India the mean life expectancy was 50 years. If the life expectancies from a random sample of 11 persons are 2 5

58.2, 56.6, 54.2, 50.4, 44.2, 61.9, 57.5, 53.4, 49.7, 55.4, 57.0

Does it confirm the expected view? Use  $t_{0.01} = 2.764$  for 4 degree of freedom.

**(ii)** During the first 13 weeks of the television season, the Saturday evening 8: 00 2 3/5

p.m. to 9: 00 p.m. audience proportions were recorded as ABC 29%, CBS 28%, NBC 25%, and independents 18%. A sample of 300 homes two weeks after a Saturday night schedule revision yielded the following viewing audience data: ABC 95 homes; CBS 70 homes, NBC 89 homes, and independents 46 homes.

Use  $\chi_{0.052}^2 = 7.81473$ .

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CO : Course Outcome Number

BTL : Blooms Taxonomy Level

Level of Bloom's Revised Taxonomy in Assessment

1: Remember	2: Understand	3: Apply
4: Analyze	5: Evaluate	6: Create